

Chemistry 132 NT

The face of a child can say it all. Especially the mouth part of the face.

Jack Handey

Chem 132 NT

Acid-Base Equilibria

Module 1

- Solutions of a Weak Acid
- Acid-Ionization Equilibria
- Polyprotic Acids



Reaction of zinc metal with hydrochloric acid.

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Review

- ✎ Identifying acid and base species
- ✎ Identifying Lewis acid and base species
- ✎ Deciding whether reactants or products are favored in an acid-base reaction
- ✎ Calculating the concentration of H^+ and OH^- in solutions of strong acid or base
- ✎ Calculating the pH from the hydrogen-ion concentration, or vice versa.

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Solutions of a Weak Acid or Base

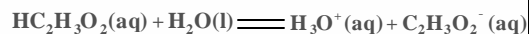
- ✎ The simplest acid-base equilibria are those in which a single acid or base solute reacts with water.
 - ◆ In this chapter, we will first look at solutions of weak acids and bases.
 - ◆ We must also consider solutions of salts, which can have acidic or basic properties as a result of the reactions of their ions with water.

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Acid-Ionization Equilibria

- ✎ **Acid ionization** (or acid dissociation) is the reaction of an acid with water to produce hydronium ion (hydrogen ion) and the conjugate base anion.

◆ When acetic acid is added to water it reacts as follows.



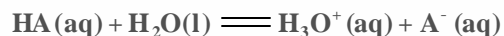
◆ Because acetic acid is a weak electrolyte, it ionizes to a small extent in water.

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Acid-Ionization Equilibria

✎ For a weak acid, the equilibrium concentrations of ions in solution are determined by the **acid-ionization constant** (also called the acid-dissociation constant).

◆ Consider the generic monoprotic acid, HA.



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Acid-Ionization Equilibria

✎ For a weak acid, the equilibrium concentrations of ions in solution are determined by the **acid-ionization constant** (also called the acid-dissociation constant).

◆ The corresponding equilibrium expression is:

$$K_c = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}][\text{H}_2\text{O}]}$$

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Acid-Ionization Equilibria

✎ For a weak acid, the equilibrium concentrations of ions in solution are determined by the **acid-ionization constant** (also called the acid-dissociation constant).

◆ Since the concentration of water remains relatively constant, we rearrange the equation to get:

$$K_a = [\text{H}_2\text{O}]K_c = \frac{[\text{H}_3\text{O}^+][\text{A}^-]}{[\text{HA}]}$$

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Acid-Ionization Equilibria

For a weak acid, the equilibrium concentrations of ions in solution are determined by the **acid-ionization constant** (also called the acid-dissociation constant).

Thus, K_a , the **acid-ionization constant**, equals the constant $[H_3O^+][A^-]$.

$$K_a = \frac{[H_3O^+][A^-]}{[HA]}$$

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Acid-Ionization Equilibria

For a weak acid, the equilibrium concentrations of ions in solution are determined by the **acid-ionization constant** (also called the acid-dissociation constant).

A table in your text lists acid-ionization constants for various weak acids. Here are a couple of examples.

Substance	Formula	K_a
Acetic acid	$HC_2H_3O_2$	1.7×10^{-5}
Hydrocyanic acid	HCN	4.9×10^{-10}

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Experimental Determination of K_a

The **degree of ionization** of a weak electrolyte is the fraction of molecules that react with water to give ions.

Electrical conductivity or some other colligative property can be measured to determine the degree of ionization.

With weak acids, the pH can be used to determine the equilibrium composition of ions in the solution.

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A Problem To Consider

◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

◆ It is important to realize that the solution was made 0.012 M in nicotinic acid, however, some molecules ionize making the equilibrium concentration of nicotinic acid less than 0.012 M.

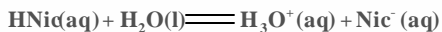
◆ We will abbreviate the formula for nicotinic acid as HNic.

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A Problem To Consider

◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

◆ Let x be the moles per liter of product formed.



Starting	0.012		
Change	-x		
Equilibrium	0.012-x		

	0	0
	+x	+x
	x	x

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A Problem To Consider

◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

◆ The equilibrium-constant expression is:

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{Nic}^-]}{[\text{HNic}]}$$

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A Problem To Consider

- ◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

- ◆ Substituting the expressions for the equilibrium concentrations, we get

$$K_a = \frac{x^2}{(0.012 - x)}$$

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A Problem To Consider

- ◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

- ◆ We can obtain the value of x from the given pH.

$$x = [\text{H}_3\text{O}^+] = \text{antilog}(-\text{pH})$$

$$x = \text{antilog}(-3.39)$$

$$x = 4.1 \times 10^{-4} = 0.00041$$

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A Problem To Consider

- ◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

- ◆ Substitute this value of x in our equilibrium expression.

- ◆ Note first, however, that

$$(0.012 - x) = (0.012 - 0.00041) = 0.01159 \approx 0.012$$

the concentration of unionized acid remains virtually **unchanged**.

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A Problem To Consider

- ◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

- ◆ Substitute this value of x in our equilibrium expression.

$$K_a = \frac{x^2}{(0.012 - x)} = \frac{(0.00041)^2}{(0.012)} = 1.4 \times 10^{-5}$$

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A Problem To Consider

- ◆ Nicotinic acid is a weak monoprotic acid with the formula $\text{HC}_6\text{H}_4\text{NO}_2$. A 0.012 M solution of nicotinic acid has a pH of 3.39 at 25 °C. **Calculate the acid-ionization constant, K_a ,** for this acid at 25 °C.

- ◆ To obtain the degree of dissociation:

$$\text{Degree of dissociation} = \frac{0.00041}{0.012} = 0.034$$

- ◆ The percent ionization is obtained by multiplying by 100, which gives 3.4%.

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Calculations With K_a

- ◆ Once you know the value of K_a , you can calculate the **equilibrium concentrations of species HA, A⁻, and H₃O⁺** for solutions of different molarities.

- ◆ The general method for doing this was discussed in our chapter on equilibrium.

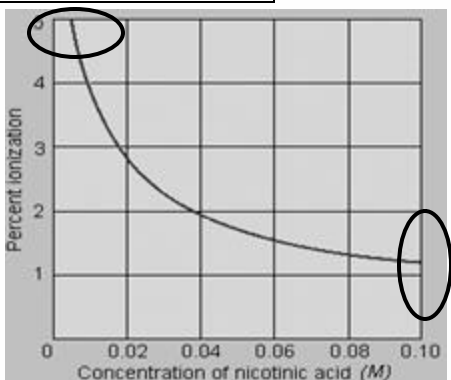
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Calculations With K_a

- ◆ Note that in our previous example, the degree of dissociation was so small that “ x ” was **negligible compared to the concentration of nicotinic acid**.
- ◆ It is the **small value of the degree of ionization that allowed us to ignore the subtracted x** in the denominator of our equilibrium expression.
- ◆ The degree of ionization of a weak acid depends on both the K_a and the concentration of the acid solution (see the figure on the next slide).

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Percent Ionization vs Acid Concentration



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Calculations With K_a

- ◆ **How do you know when you can use this simplifying assumption?**
 - ◆ It can be shown that if the acid concentration, C_a , divided by the K_a exceeds 100, that is,
$$\text{if } \frac{C_a}{K_a} > 100$$
then this simplifying assumption of **ignoring the subtracted x** gives an **acceptable error of less than 5%**.

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Calculations With K_a

◆ **How do you know when you can use this simplifying assumption?**

- ◆ If the simplifying assumption is **valid**, you can approximate the equilibrium calculations by ignoring added or subtracted “x”s in the equilibrium expression.
- ◆ The next example illustrates this with a solution of nicotinic acid, again.

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A Problem To Consider

◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

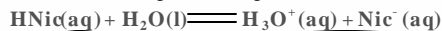
- ◆ As in our previous example, the solution was made 0.10 M in nicotinic acid, however, some molecules ionize making the equilibrium concentration of nicotinic acid less than 0.10 M.
- ◆ We will again abbreviate the formula for nicotinic acid as HNic.

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A Problem To Consider

◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- ◆ Let x be the moles per liter of product formed.



Starting	0.10		0		0
Change	-x		+x		+x
Equilibrium	0.10-x		x		x

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A Problem To Consider

- ◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- ◆ The equilibrium-constant expression is:

$$K_a = \frac{[\text{H}_3\text{O}^+][\text{Nic}^-]}{[\text{HNic}]}$$

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A Problem To Consider

- ◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- ◆ Substituting the expressions for the equilibrium concentrations, we get

$$K_a = \frac{x^2}{(0.10 - x)} = 1.4 \times 10^{-5}$$

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A Problem To Consider

- ◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- ◆ Here is where we must decide whether we can simplify the equation or if we must solve the quadratic.

$$K_a = \frac{x^2}{(0.10 - x)} = 1.4 \times 10^{-5}$$

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- Divide the acid concentration by the K_a .

$$\frac{C_a}{K_a} = \frac{0.10 \text{ M HNic}}{1.4 \cdot 10^{-5}} = 7143$$

which is much greater than 100, so we can use our **simplifying assumption that x will be negligible**.

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- This means that “x” is so much smaller than the 0.10 M HNic concentration, that subtracting it from 0.10 won’t change the value.

- That is,

$$0.10 - x @ 0.10$$

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- Going back to our equilibrium expression, we see

$$K_a = \frac{x^2}{(0.10 - x)} = 1.4 \cdot 10^{-5} @ \frac{x^2}{(0.10)}$$

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- Solving for x

$$x^2 @ (1.4 \times 10^{-5}) \cdot (0.10) @ 1.4 \times 10^{-6}$$
$$x @ 1.2 \times 10^{-3} = 0.0012$$

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- Checking to see if our simplifying assumption was correct, we see that

$$0.10 - x = (0.10 - 0.0012) = 0.10$$

(to two significant figures)

the assumption was indeed valid.

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A Problem To Consider

- What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- We can now find the equilibrium concentrations of all the species by substituting x into the last line of our original table.

- The concentrations of **HNic**, **H⁺**, and **Nic⁻** are **0.10 M**, **0.0012 M**, and **0.0012 M**, respectively.

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A Problem To Consider

- ◆ What are the concentrations of **nicotinic acid**, **hydrogen ion**, and **nicotinate ion** in a solution of 0.10 M nicotinic acid, $\text{HC}_6\text{H}_4\text{NO}_2$, at 25°C ? What is the **pH** of the solution? The acid ionization constant, K_a , is 1.4×10^{-5} .

- ◆ The pH of the solution is

$$\text{pH} = -\log[\text{H}^+] = -\log(0.0012) = 2.92$$

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Calculations With K_a

- ◆ How do you know when you can use this simplifying assumption?

- ◆ If the simplifying assumption is **not valid**, you can solve the equilibrium equation exactly by using the **quadratic equation**.
- ◆ The next example illustrates this with a solution of aspirin (acetylsalicylic acid), $\text{HC}_9\text{H}_7\text{O}_4$, a common headache remedy.

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A Problem To Consider

- ◆ What is the **pH** at 25°C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25°C .

- ◆ The molar mass of $\text{HC}_9\text{H}_7\text{O}_4$ is 180.2 g.

From this we find that the sample contained 0.00180 mol of the acid.

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ The molar mass of $\text{HC}_9\text{H}_7\text{O}_4$ is 180.2 g.

Hence, the concentration of the acetylsalicylic acid is $0.00180 \text{ mol}/0.500 \text{ L} = \mathbf{0.0036 \text{ M}}$ (Retain two significant figures, the same number of significant figures in K_a).

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ Note that

$$\frac{C_a}{K_a} = \frac{0.0036}{3.3 \times 10^{-4}} = 11$$

which is less than 100, so **we must solve the equilibrium equation exactly.**

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ We will abbreviate the formula for acetylsalicylic acid as **HAcs** and let **x** be the amount of H_3O^+ formed per liter.

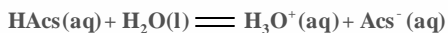
◆ The amount of acetylsalicylate ion is also **x** mol; the amount of nonionized acetylsalicylic acid is **(0.0036-x)** mol.

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ These data are summarized below.



Starting	0.0036
Change	-x
Equilibrium	0.0036-x

0	0
+x	+x
x	x

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ The equilibrium constant expression is

$$\frac{[\text{H}_3\text{O}^+][\text{AcS}^-]}{[\text{HAcS}]} = K_a$$

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ If we substitute the equilibrium concentrations and the K_a into the equilibrium constant expression, we get

$$\frac{x^2}{(0.0036 - x)} = 3.3 \times 10^{-4}$$

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a=3.3 \times 10^{-4}$ at 25 °C.

◆ You can solve this equation exactly by using the quadratic formula.

◆ Rearranging the preceding equation to put it in the form $ax^2 + bx + c = 0$, we get

$$x^2 + (3.3 \times 10^{-4})x - (1.2 \times 10^{-6}) = 0$$

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a=3.3 \times 10^{-4}$ at 25 °C.

◆ Now substitute into the quadratic formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

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A Problem To Consider

◆ **What is the pH** at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a=3.3 \times 10^{-4}$ at 25 °C.

◆ Now substitute into the quadratic formula.

$$x = \frac{-(3.3 \times 10^{-4}) \pm \sqrt{(3.3 \times 10^{-4})^2 - 4(1.2 \times 10^{-6})}}{2}$$

◆ The lower sign in \pm gives a negative root which we can ignore.

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A Problem To Consider

◆ What is the pH at 25 °C of a solution obtained by dissolving 0.325 g of acetylsalicylic acid (aspirin), $\text{HC}_9\text{H}_7\text{O}_4$, in 0.500 L of water? The acid is monoprotic and $K_a = 3.3 \times 10^{-4}$ at 25 °C.

◆ Taking the upper sign, we get

$$x = [\text{H}_3\text{O}^+] = 9.4 \times 10^{-4}$$

◆ Now we can calculate the pH.

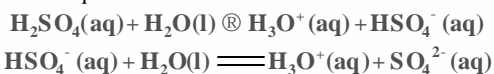
$$\text{pH} = -\log(9.4 \times 10^{-4}) = 3.03$$

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Polyprotic Acids

⚠ Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

◆ Sulfuric acid, for example, can lose two protons in aqueous solution.



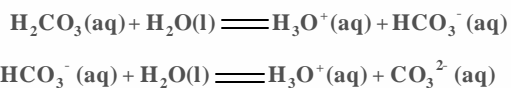
◆ The first proton is lost completely followed by a weak ionization of the hydrogen sulfate ion, HSO_4^- .

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Polyprotic Acids

⚠ Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

◆ For a weak diprotic acid like carbonic acid, H_2CO_3 , two simultaneous equilibria must be considered.



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Polyprotic Acids

Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

- Each equilibrium has an associated acid-ionization constant.

For the loss of the **first** proton

$$K_{a1} = \frac{[\text{H}_3\text{O}^+][\text{HCO}_3^-]}{[\text{H}_2\text{CO}_3]} = 4.3 \cdot 10^{-7}$$

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Polyprotic Acids

Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

- Each equilibrium has an associated acid-ionization constant.

For the loss of the **second** proton

$$K_{a2} = \frac{[\text{H}_3\text{O}^+][\text{CO}_3^{2-}]}{[\text{HCO}_3^-]} = 4.8 \cdot 10^{-11}$$

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Polyprotic Acids

Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

- In general, the second ionization constant, K_{a2} , for a polyprotic acid is smaller than the first ionization constant, K_{a1} .
- In the case of a triprotic acid, such as H_3PO_4 , the third ionization constant, K_{a3} , is smaller than the second one, K_{a2} .

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Polyprotic Acids

Some acids have two or more protons (hydrogen ions) to donate in aqueous solution. These are referred to as **polyprotic acids**.

- When several equilibria occur at once, it might appear complicated to calculate equilibrium compositions.
- However, reasonable assumptions can be made that simplify these calculations as we show in the next example.

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A Problem To Consider

Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?

The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- For diprotic acids, K_{a2} is so much smaller than K_{a1} that the smaller amount of hydronium ion produced in the second reaction **can be neglected**.

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A Problem To Consider

Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?

The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

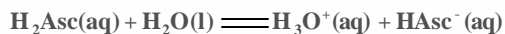
- The pH can be determined by simply solving the equilibrium problem posed by the first ionization.

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

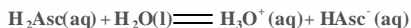
◆ If we abbreviate the formula for ascorbic acid as H_2Asc , then the first ionization is:



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A Problem To Consider

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The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.



Starting	0.10
Change	-x
Equilibrium	0.10-x

0	0
+x	+x
x	x

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

◆ The equilibrium constant expression is

$$\frac{[\text{H}_3\text{O}^+][\text{HAsc}^-]}{[\text{H}_2\text{Asc}]} = K_{a1}$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ Substituting into the equilibrium expression

$$\frac{x^2}{(0.10 - x)} = 7.9 \times 10^{-5} @ \frac{x^2}{0.10}$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ Assuming that x is much smaller than 0.10, you get

$$x^2 @ (7.9 \times 10^{-5}) \cdot (0.10)$$
$$x @ 2.8 \times 10^{-3} = 0.0028$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ The hydronium ion concentration is 0.0028 M, so

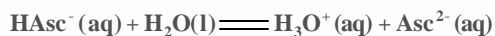
$$\text{pH} = -\log(0.0028) = 2.55$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ The ascorbate ion, Asc^{2-} , which we will call "y", is produced only in the second ionization of H_2Asc .

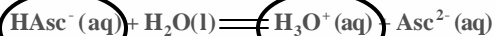


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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

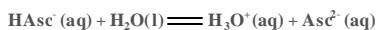
- ◆ Assume the starting concentrations for HAsc^- and H_3O^+ to be those from the first equilibrium.



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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.



Starting	0.0028	0.0028	0
Change	-y	+y	+y
Equilibrium	0.0028-y	0.0028+y	y

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ The equilibrium constant expression is

$$\frac{[\text{H}_3\text{O}^+][\text{Asc}^{2-}]}{[\text{HAsc}^-]} = K_{a2}$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ Substituting into the equilibrium expression

$$\frac{(0.0028 + y)(y)}{(0.0028 - y)} = 1.6 \times 10^{-12}$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$? The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

- ◆ Assuming y is much smaller than 0.0028, the equation simplifies to

$$\frac{(0.0028)(y)}{(0.0028)} @ 1.6 \times 10^{-12}$$

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A Problem To Consider

- ◆ Ascorbic acid (vitamin C) is a diprotic acid, $\text{H}_2\text{C}_6\text{H}_6\text{O}_6$. **What is the pH** of a 0.10 M solution? What is the concentration of the ascorbate ion, $\text{C}_6\text{H}_6\text{O}_6^{2-}$?
The acid ionization constants are $K_{a1} = 7.9 \times 10^{-5}$ and $K_{a2} = 1.6 \times 10^{-12}$.

◆ Hence, $y @ [\text{Asc}^{2-}] = 1.6 \times 10^{-12}$

- ◆ The concentration of the ascorbate ion equals K_{a2} .

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Operational Skills

- ✎ Determining K_a (or K_b) from the solution pH
- ✎ Calculating the concentration of a species in a weak acid solution using K_a
- ✎ Calculating concentrations of species in a solution of a diprotic acid

Time for a few review questions

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